## Greatest common divisor Least common multiple

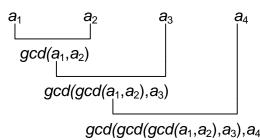
**E-OLYMP <u>137. GCD</u>** Find the Greatest Common Divisor of *n* numbers.

► It is known that

GCD  $(a_1, a_2, ..., a_i) =$  GCD (GCD  $(a_1, a_2, ..., a_{i-1}), a_i)$ 

We shall sequentially calculate the greatest common divisor of two, three,..., n numbers. For example, for four numbers holds an equality:

GCD  $(a_1, a_2, a_3, a_4) =$  GCD (GCD (GCD (GCD  $(0, a_1), a_2), a_3), a_4)$ 



Ler *res* be the Greatest Common Divisor of *n* numbers. Initialize it with 0. Read the input data and sequentially find GCD of *n* numbers.

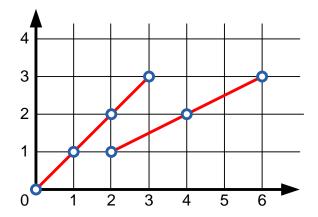
```
res = 0;
scanf("%d", &n);
while (n--)
{
    scanf("%d", &b);
    res = gcd(res, b);
}
```

**E-OLYMP** <u>7363. GCD</u> Find the sum of two proper fractions a / b and c / d. Give the result in the form of irreducible fraction. If the result is an integer, print this one integer.

• It's obvious that  $\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$ . It remains to simplify the resulting fraction

by their greatest common divisor.

**E-OLYMP** <u>136. The segment</u> The segment's end points have integer coordinates. Find the number of points on a segment with integer coordinates.



► If  $(x_1, y_1)$  and  $(x_2, y_2)$  are ends of a segment with integer coordinates, then it contains  $1 + \text{GCD}(|x_2 - x_1|, |y_2 - y_1|)$  points with integer coordinates.

For the first sample input the answer is

1 + GCD (|3 - 0|, |3 - 0|) = 1 + GCD (3, 3) = 1 + 3 = 4For the second sample input the answer is 1 + GCD (|6 - 2|, |3 - 1|) = 1 + GCD (4, 2) = 1 + 2 = 3

**E-OLYMP** <u>6941. Sum of GCD</u> Given n positive integers, you have to find the summation of GCD (greatest common divisor) of every possible pair of these integers.

For each test case, put the input numbers into mas array. Next, for each pair (*i*, *j*)  $(0 \le i < j < m)$  calculate the GCD (mas[*i*], mas[*j*]) and add it to the overall sum.

s = 0; for (i = 0; i < m; i++) for (j = i + 1; j < m; j++) s += gcd(mas[i], mas[j]);